

1 **Observations and modeling of ice cloud shortwave spectral albedo during the**
2 **Tropical Composition, Cloud and Climate Coupling Experiment**

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42 **Abstract**

43

44 Ice cloud optical thickness and effective radius is retrieved from hyperspectral irradiance
45 and discrete spectral radiance measurements for four ice cloud cases during TC⁴ over a
46 range of solar zenith angle (23 ° to 53°) and high (46-90) and low (5-15) optical
47 thicknesses. The retrieved optical thickness and effective radius using measurements at
48 only two wavelengths from the Solar Spectral Flux Radiometer (SSFR) Irradiance and
49 the MODIS Airborne Simulator (MAS) was input to a radiative transfer model using two
50 libraries of ice crystal single scattering optical properties to reproduce spectral albedo
51 over the spectral range from 400 to 2130 nm. The two commonly used ice single
52 scattering models were evaluated by examining the residuals between observed spectral
53 and predicted spectral albedo. The SSFR and MAS retrieved optical thickness and
54 effective radius were in close agreement for the low to moderately optically thick clouds
55 with a mean difference of 3.42 in optical thickness (SSFR lower relative to MAS) and
56 3.79 μm in effective radius (MAS smaller relative to SSFR). The higher optical
57 thickness case exhibited a larger difference in optical thickness (40.5) but nearly identical
58 results for effective radius. The single scattering libraries were capable of reproducing the
59 spectral albedo in most cases examined to better than 0.05 for all wavelengths.
60 Systematic differences between the model and measurements increased with increasing
61 optical thickness and approached 0.10 between 400-600 nm and selected wavelengths
62 between 1200-1300 nm. Differences between radiance- and irradiance-based retrievals of
63 optical thickness and effective radius error sources in the modeling of ice single
64 scattering properties are examined.

65

66 **1. Introduction**

67 Ice clouds play an important role in the radiative budget of the Earth's atmosphere
68 [*Chen et al.*, 2000, *Ramanathan et al.*, 1989] for example. The scattering and absorption
69 of solar radiation reduces the amount of energy reaching the surface and thus has a
70 cooling effect. Conversely, in the terrestrial thermal infrared wavelengths, ice clouds
71 absorb radiation and emit at a lower temperature than the Earth's lower atmosphere and
72 surface. This reduces the amount of energy radiated to space, increases the downward
73 infrared radiation, and warms the surface. Whether ice cloud net effect is cooling or
74 heating is dependent on several factors including cloud height, cloud thickness, and cloud
75 microphysics [*Stephens et al.*, 1990, *Ebert and Curry*, 1992; *Jensen et al.*, 1994], for
76 example. Ice cloud microphysical and optical properties that determine the radiative
77 properties of clouds are perhaps the least well understood of these.

78 Liquid water cloud radiative transfer calculations utilize Lorenz-Mie theory, an
79 exact computational method for calculating the single scattering properties (e.g. single
80 scattering albedo and phase function or its first moment asymmetry parameter) of
81 homogeneous spheres. In contrast to liquid water droplets, non-spherical ice cloud
82 particles encompass a wide variety of shapes and sizes and thus computing their radiative
83 properties must rely on more involved numerical techniques. To this end, extensive
84 modeling and some measurements of ice crystal single scattering properties have been
85 undertaken [*Takano and Liou*, 1989; *Macke et al.*, 1996; *Baum et al.*, 2005; *Yang and*
86 *Liou* 1998; *Yang et al.* 2003; *Yang et al.*, 1997; *Mishchenko et al.*, 1996] and continues to
87 be an area of active research. These models are used for satellite remote sensing retrievals
88 of cloud optical properties (e.g. MODIS, AVHRR, etc) [*King et al.*, 1992; *Platnick et al.*,

89 2003]. Ultimately, these types of satellite retrievals are used: as inputs to climate models
90 to properly parameterize ice cloud radiative effects [Stephens, *et al.*, 1990], to potentially
91 improve ice water parameterization in global circulation models [Waliser, *et al.*, 2009],
92 and to aid in the study of ice cloud processes [Jiang, *et al.*, 2009].

93 Satellite remote sensing retrievals are, by necessity, radiance based and
94 implement observations from discrete wavelength bands distributed across the solar and
95 terrestrial spectrum. A selection of channels from radiance-based remote sensing
96 instruments is, by itself, insufficient to completely determine the effects of clouds on the
97 Earth's radiation budget. In practice, irradiance cannot be measured directly from space-
98 borne platforms in low Earth orbit. It is, however, measured from aircraft. To bridge the
99 fundamental geometrical and spectral differences between satellite measurements of
100 discrete-band radiance and the more energetically relevant quantity, continuous spectral
101 irradiance, field campaigns deploying instruments that measure discrete-band radiance
102 and hyperspectral irradiance have been conducted: the Ice Regional Study of Tropical
103 Anvils and Cirrus Layers-Florida Area Cirrus Experiment (CRYSTAL-FACE) [Jensen *et*
104 *al.*, 2004]; and the focus of the present study, the Tropical Composition, Cloud and
105 Climate Coupling experiment (TC⁴) [Toon summary paper, this collection, 2009]. In TC⁴
106 the high altitude NASA ER-2 flew with the Solar Spectral Flux Radiometer (SSFR),
107 which measured spectrally continuous solar irradiance, and the MODIS Airborne
108 Simulator (MAS), a discrete-band imaging spectrometer that measured solar reflected
109 radiance.

110 Simultaneous and co-located observations from these two instruments over
111 tropical ice cloud layers helped to address several important questions regarding ice cloud

112 radiative transfer: How well do current models of ice crystal single scattering properties
113 reproduce the measured shortwave spectral albedo of ice clouds encountered during TC⁴?
114 Are systematic errors evident from the comparisons? How well do the retrieved values of
115 optical thickness and effective radius retrieved from satellite-like measurements (MAS)
116 reproduce the measured spectral albedo? Are there significant differences in ice retrievals
117 between radiance-based and irradiance-based methods?

118 One of the main purposes of this study was to examine how well the models of
119 single scattering optical properties of ice particles can reproduce the spectral albedo of
120 ice clouds encountered during TC⁴. Satellite retrievals of cloud optical thickness and
121 effective radius are typically retrieved at just two spectral bands, one in the visible to very
122 near-infrared where ice and liquid water are non-absorbing and the other in the shortwave
123 -infrared where ice and liquid water weakly absorb. The former is most sensitive to
124 cloud optical thickness, the latter to cloud particle size. For a complete description of this
125 type of retrieval see, for example, *Twomey and Cocks* [1989] or *Nakajima and King*
126 [1990].

127 Current models of ice single scattering properties contain far more than two
128 wavelengths. The models used in this study contains 140-150 wavelengths [*Yang and*
129 *Liou, 1998; Baum et al., 2005*] spread across the solar spectrum. In principle, if the
130 model of the single scattering is spectrally accurate, then the retrieved optical thickness
131 and effective radius from as few as two wavelengths should accurately predict the
132 spectral albedo for the entire spectrum. By retrieving the optical properties of ice clouds,
133 using the classical two wavelength technique, one should be able to test, at the very least,

134 how consistent the wavelength to wavelength albedo is modeled by comparing with
135 spectral measurements of albedo from the SSFR.

136 The effects of cloud vertical [Platnick, 2000,] and horizontal [Platnick, 2001;
137 Eichler et al., 2009] inhomogeneity on the retrieval of cloud optical properties have been
138 investigated previously. For clouds with varying vertical and or horizontal microphysical
139 structure, the use of different wavelengths in the inversion procedures may result in
140 different values of retrieved effective radius. However, these differences are typically
141 small compared to retrieval errors. In this paper, all calculations were done for plane-
142 parallel, homogenous (vertically and horizontally) clouds. The impact of vertical and/or
143 horizontal cloud inhomogeneities on retrievals of optical thickness and effective radius
144 was not investigated in this work.

145 Because many remote sensing retrievals of cloud optical thickness and effective
146 radius rely on these single particle scattering models testing their spectral fidelity is an
147 important validation. The accuracy of the models cannot be judged solely from remote
148 sensing measurements as it implies some level of circularity. It would be preferable, for
149 instance, to have an independent measurement of particle size. Particle size
150 measurements, *in situ*, were made during TC⁴, but are prone to crystal shattering
151 [McFarquhar et al., 2007; Jensen et al., 2009]. Even in the absence of *in situ*
152 measurement errors like inlet shattering, issues of cloud volume sampling -small and
153 usually deep within a cloud for *in situ* measurements-large and near cloud top for
154 radiation measurements also confound efforts at comparing the two. For these reasons, no
155 *in situ* data were used.

156 A previous study was conducted in a similar vein, comparing solar wavelengths
157 with thermal wavelengths and found the two regions to have inconsistencies [*Baran and*
158 *Francis, 2004*]. Here we have examined the spectral consistency at high spectral
159 resolution and sampling over the majority of the solar spectrum, at optical thicknesses
160 ranging from 3 to 46 and solar zenith angles ranging from 23° to 53° . The differences
161 between measured spectral albedo, and predicted spectral albedo derived from ice single
162 scattering properties are discussed as are the differences in the retrieval from radiance
163 and irradiance based measurements used in this study.

164 This paper is organized as follows: (1) the measurements of spectral irradiance
165 from the SSFR and radiance imagery from MAS, (2) models of single scattering optical
166 properties and their incorporation into a radiative transfer model along with the method
167 employed for retrieving the optical thickness, effective radius, and albedo, (3) cloud
168 optical thickness and effective radius retrieved from MAS radiance and SSFR irradiance
169 using two currently available ice single scattering libraries, (4) the spectral albedo
170 calculated from a two-wavelength SSFR retrieval compared with the measured spectral
171 albedo and also the spectral albedo calculated from a two-wavelength MAS radiance
172 retrieval compared with the measured spectral albedo, (5) individual spectra for high and
173 low optical thickness and effective radius from each case, and (6) a summary of the work.

174 **2. Measurements of Radiance and Irradiance during TC⁴**

175 The NASA ER-2 was instrumented with the SSFR and either the MAS [*King et al., 2004*]
176 or the MODIS/ASTER airborne simulator [*Hook et al., 2001*] for thirteen flights together
177 over the course of the experiment. These flights covered a wide variety of cloud types,
178 including extensive fields of low marine stratus, tropical convective systems, and high

179 tropical ice clouds-the focus of this paper. The NASA DC-8 was also equipped with a
180 SSFR, and coordinated flights with the ER-2 took place on several occasions, with the
181 DC-8 flying below a cloud deck and the ER-2 above. Coordinated aircraft flight above
182 and below a cloud layer enables the measurement of flux divergence or cloud absorption.
183 This is the subject of a companion paper in this volume [*Schmidt et al.*, 2009]. Here we
184 focus solely on the reflected solar radiation at cloud top.

185 **2.1 Solar Spectral Flux Radiometer (SSFR)**

186 The SSFR consists of two spectroradiometers connected via a fiber optic to a miniature
187 integrating sphere mounted on the top (zenith viewing) and bottom (nadir viewing) of the
188 NASA ER-2. The integrating spheres provide the cosine response over the wide
189 wavelength range of the SSFR that is required to make a measurement of spectral
190 irradiance. The wavelength range of the instrument, 350 to 2150 nm, encompasses 90%
191 of incident solar radiation. The spectral resolution as measured by the full-width-half-
192 maximum (FWHM) of a line source is 8 nm from 400 to 1000 nm with 3 nm sampling
193 and 12 FWHM from 1000 to 2200 nm with 4.5 nm sampling. The SSFR records a nadir
194 and zenith spectrum every second.

195 The spectrometers are calibrated in the laboratory with a NIST-traceable
196 blackbody (tungsten-halogen 1000W bulb). The radiometric stability of the SSFR is
197 carefully tracked during the course of a field experiment with a portable field calibration
198 unit with a highly stable power source and 200W lamps. The calibration has generally
199 held to the 1 to 2% level over the course of a several week field mission as it did during
200 TC⁴. The radiometric calibration was adjusted for minor fluctuations measured by the
201 field calibration from flight to flight. In addition, the data were filtered using the aircraft

202 navigation and ephemeris data to eliminate time periods when the aircraft attitude was
203 not level (e.g. turns, takeoff and landing, turbulence). The estimated uncertainties in the
204 absolute calibration of the instrument are 5%. We note that when retrieving cloud optical
205 properties with albedos, as was done here, error in the absolute calibration cancel. Errors
206 from unknown offsets in aircraft navigation data or reflections from clouds may remain
207 however. For a more complete description of the SSFR instrument see [*Pilewskie et al.*,
208 2003].

209 **2.2 MODIS Airborne Simulator (MAS)**

210 The MAS instrument is an imaging spectrometer with 50 discrete bands
211 distributed throughout the solar reflected and thermal emitted parts of the spectrum.
212 Twenty-two of the bands in the solar region overlap with the SSFR from 461 to 2213 nm.
213 The spectral bandpass of MAS in the visible and near-infrared channels are in the range
214 of 40-50 nm, it has a 2.5 mrad instantaneous field of view (IFOV), and 16-bit analog to
215 digital conversion. MAS is typically pre- and post-flight calibrated in the laboratory with
216 an integrating sphere and uses an integrating hemisphere in the field for stability
217 monitoring. For details on MAS calibration issues and investigations during TC⁴, see
218 King et al., Because it is an imager, it provides excellent spatial context (~25 m nadir
219 pixel resolution with ~17 km swath width for typical TC4 ice cloud heights) with which
220 to help interpret the measurements of irradiance from SSFR.

221 All thirteen flights and all flight legs therein were examined with the MAS cloud
222 product which includes cloud optical thickness, cloud phase, cloud top height, and
223 temperature information. The flight legs used in this study were selected based on
224 several criteria: the abundance of ice clouds; legs that were only over open ocean to

225 simplify the input of surface spectral albedo into the radiative transfer calculations; the
226 apparent absence of low level clouds which might make the retrieval of ice cloud
227 properties more complicated and prone to error (an example of this which occurred
228 frequently in the data are low level cumulus clouds, presumably liquid water, beneath an
229 optically thin layer of ice cloud); and finally, stable, level flight which is required for the
230 measurement of irradiance. Four flight tracks from 17 July 2007 met these criteria and
231 were used for analysis in this work. The cosine of the mean solar zenith angles (denoted
232 by μ) for the four flight legs were 0.60, 0.82, 0.88, and 0.92. For the remainder of this
233 paper the four cases will be distinguished by their cosine of solar zenith angle. (i.e. the
234 $\mu=0.82$ case, the $\mu=0.88$ case, etc). Of these cases three ($\mu=0.60, 0.82, 0.88$) had low to
235 moderate optical thickness (3-15) and one case ($\mu=0.92$) had high optical thickness (40-
236 50)

237 **2.3 Radiative Transfer Calculations of Irradiance**

238 Analysis of solar spectral irradiance from SSFR has lead to the development of a
239 radiative transfer code optimized for the spectral characteristics of the SSFR and for
240 flexibility in specifying cloud and aerosol radiative properties [*Bergstrom et al.*, 2003;
241 *Coddington et al.*, 2008] The molecular absorption by species such as water vapor,
242 oxygen, ozone, and carbon dioxide, are calculated using the correlated-k method [*Lacis*
243 *and Oinas*, 1991]. The band model was developed specifically for the SSFR by defining
244 the spectral width of the bands by the slit function of the SSFR spectrometers, the half-
245 widths of which were noted previously. The k-distribution is based on the HITRAN 2004
246 high resolution spectroscopic database [*Rothman et al.*, 2005]. The model uses the
247 discrete ordinate radiative transfer method (DISORT) [*Stamnes et al.*, 1988] to solve for

248 the spectral irradiance and nadir and zenith radiance at each level. Molecular scattering
249 optical thickness is calculated using the analytical method of Bodhaine [*Bodhaine et al.*,
250 1999]. The model contains 36 levels. In this study albedo was calculated at 20 km, the
251 nominal flight level of the ER-2. The albedo is defined as the ratio of upwelling to
252 downwelling irradiance at the flight level. A standard tropical atmospheric profile of
253 water vapor and well mixed radiatively active gases was used. No attempt was made to
254 fit the water vapor amount to match the measurements; this would be computationally
255 prohibitive and unnecessary, because the absorption bands of water vapor, oxygen, etc.
256 are avoided for inferring cloud optical properties. Clouds heights for these cases were
257 examined using the MAS cloud height product and were found to vary from between 8 to
258 12 km. A cloud height sensitivity test was performed by setting a cloud deck to 12 and to
259 8 km, for the retrieval of cloud optical properties. Little to no change in the retrieved
260 values was found, so that the calculation was set to 10km for all of the cases. This is the
261 result of using 870 nm as one of the retrieval wavelengths. The molecular scattering is
262 reduced at this wavelength and the effect on the retrieval of cloud height was small. The
263 use of a shorter wavelength (e.g. 500 nm) would likely show a greater sensitivity to cloud
264 height.

265 The ice crystal single scattering models used here are the same ones used for the
266 MODIS Collection 4 [*Baum et al.*, 2000; *Platnick et al.*, 2003; *Yang and Liou*, 1996;
267 henceforth C4] and Collection 5 cloud products [*Baum et al.*, 2005, henceforth C5]. The
268 C5 models consist of plates, hollow and solid columns, 2-D bullet rosettes, and
269 aggregates consisting of solid columns. These early models provide scattering properties
270 for 5 size bins and were integrated over 12 particle size distributions. The C5 models

271 consist of mixtures of different ice particle shapes (e.g. droxtals, solid and hollow
272 columns, plates, 3-D bullet rosettes, and aggregates of columns). The scattering
273 properties for each of these particles are available for 45 individual size bins. For both
274 sets of bulk models, all particles are smooth except for the aggregate, which is
275 roughened. Each size regime in the models consists of a different mixture; the smallest
276 consists of only droxtals, and the largest is predominantly bullet rosettes. Intermediate
277 sizes are varying mixtures of shapes.

278 The single scattering properties include a scattering phase function defined at 498
279 angles between 0^0 and 180^0 , asymmetry parameter, extinction efficiency, extinction and
280 scattering cross sections, single scattering albedo, and a delta transmission factor. The
281 delta transmission factor is wavelength dependent and is used to scale the input optical
282 thickness and single scattering albedo according to equations 1 and 2.

283

$$\tau' = (1 - \delta\varpi_0)\tau$$

284 Eq. 1.

285

$$\varpi_0' = \frac{(1 - \delta)\varpi_0}{1 - \delta\varpi_0}$$

286 Eq. 2.

287

288 where δ is the delta transmission factor, τ is the optical thickness, and ϖ_0 is the single-
289 scattering albedo. The primed quantities are the δ -scaled values of optical thickness and
290 single scattering albedo. The δ -transmission factor is used to account for transmission
291 through plane parallel ice particle planes in the forward direction i.e. at a scattering angle
292 of zero degrees [Takano and Liou, 1989]. The effective radius is defined by equation 3.

293 where $\langle V \rangle$ is the mean particle volume and $\langle A \rangle$ is the projected area for the ice crystal
294 size distribution [Mitchell, 2002].

295 Eq. 3.
$$r_{eff} = \frac{3 \langle V \rangle}{4 \langle A \rangle}$$

296 For C5 the ice particles range in size from 5 to 90 microns in a step size of ten microns
297 for a total of eighteen different effective radii. The wavelength coverage is from 400 to
298 2200 nm, matching the SSFR coverage. The database contains some spectral gaps, in the
299 regions 1000 -1200 nm, 1700 -1800 nm, and 1950-2050 nm. Outside of the gaps the
300 spectral sampling is 10 nm. The results from an earlier library, C4, used in the MODIS
301 collection 4 [Platnick *et al.*, 2003] are also shown. It has continuous spectral coverage
302 from 400 to 1695 nm. The range of effective radii in C4 is 6.7 to 59 μm with a total of
303 twelve effective radii. The small particles in C4 are assumed to be compact hexagonal
304 ice particles, unlike the smallest particles in C5 which are assumed to be droxtals [Yang
305 *et al.*, 2007]. The relative contribution of each particle shape to the size distribution is
306 also different between C5 and C4; Yang *et al.* [2007] gives a detailed summary of each.

307 The input to the radiative transfer model first requires that the phase function be
308 represented in terms of a Legendre polynomial series where the number of terms is set to
309 the number of streams used in the DISORT calculation. All of the DISORT calculations
310 for this study were done with 16 streams with Delta-M scaling [Wiscombe, 1977] to
311 account for the strong forward scattering peak in the phase function typical of large size
312 parameters. For the accurate calculation of irradiance at least six streams are required;
313 streams are the number of quadrature points in the angular integration of scattering. We
314 used the technique of Hu *et al.* [2000] to fit the phase function with the Legendre
315 coefficients for input into the radiative transfer code.

316 The panel on the left hand side of Figure 1. shows an example of the library phase
317 function at 870 nm for the largest (solid line) and smallest (dash-dot line) effective radii
318 in C5. On the right hand panel of Figure 1 the single scattering albedo wavelength
319 spectra of a smallest and largest size effective radii (C5) are shown. The phase function
320 for the largest size exhibits ice halo features at 22 and 46 degrees; the phase function for
321 the smallest particle size is notably smoother. In the shortwave-infrared the single
322 scattering albedo for the largest size is reduced below that of the smallest size, as
323 expected from simple geometric optics [Bohren and Huffman, 1983]. This forms the basis
324 for the retrieval of effective radius in this spectral regime. Ice is essentially non-absorbing
325 in the visible. No aerosol was included in the model as these are tropical, high level
326 clouds, and are unlikely to contain much aerosol. The top of the atmosphere (TOA) solar
327 spectrum is given by the Kurucz spectrum *Kurucz* [1992]. The surface albedo (always
328 ocean) was specified by constant value of 0.03. To generate an albedo library for each
329 case, a series of cloud optical thicknesses, thirty in total, were calculated for each of the
330 four solar zenith angles. Optical thickness step sizes range from 0.5 at the smallest optical
331 thickness, to 2 to 5, at intermediate optical thickness, and 10 at the highest optical
332 thickness (50-100). The resolution in the calculation of the various effective radii was
333 given by the single scattering ice library employed; eighteen in the case of the C5, twelve
334 for the C4 library. The C4 library is not evenly spaced in effective radius; it contains
335 finer sampling in the range of 25 to 40 μm . At this resolution, the spectra are sufficiently
336 smooth so they can be interpolated with a high degree of accuracy to generate a finer
337 optical thickness and effective radius grid. The optical thickness grid was linearly
338 interpolated to increments of 0.1 from endpoints of the calculations, 0-100. The effective

339 radii were linearly interpolated to a step size of 0.2 from the range of 5 to 90 μm in the
340 C5 library and 6.7 μm to 59 μm in the C4 library. Figure 2 shows a range of optical
341 thickness and effective radius of the calculated albedo spectra. The optical thicknesses
342 are color coded and the effective radii are line style coded. Note that the spectra group by
343 color in wavelengths between 400 and 1000 nm and contain information about optical
344 thickness; the spectra cluster by line style for the wavelengths 1500 to 2150 nm, and
345 contain information about effective radius.

346

347 **3. Retrieval of optical thickness and effective radius from SSFR and MAS**

348 For the retrieval of optical thickness and effective radius at least two wavelengths are
349 chosen to determine a best fit to the calculated spectra. Previous work with retrievals
350 from the SSFR has included up to five wavelengths [*Coddington et al.*, 2008]. Others
351 have investigated the utility of including more than two wavelengths [*Cooper et al.*,
352 2006]. Because wavelength selection was not the focus of this study we have chosen to
353 follow the technique used in satellite retrievals and use the MAS wavelengths 870nm
354 (water non-absorbing) and 1600 nm or 2130 nm (water absorbing). Measurement to
355 measurement variation was smaller at 1600 nm, so it was chosen for the water-absorbing
356 wavelength applied in this analysis. A two step process was implemented as follows. The
357 first step is an initial estimate from the uninterpolated data to determine the range that the
358 measurement falls in; that range is used to constrain the retrieval in the interpolated data.
359 This greatly increases the speed at which a minimum in the least squares fit is found, over
360 the search of the entire high resolution library for each measurement. The “best-fit” is

361 determined by minimizing the residual in a least squares sense (Equation 4), of the
362 measurement to calculated albedo value at the given wavelengths.

363

364 Eq.4.
$$residual = (vis_{measured} - vis_{modeled})^2 + (nir_{measured} - nir_{modeled})^2$$

365

366 The calculation of optical thickness and effective radius for MAS is given by the MAS
367 algorithm [King *et al.*, 2004] and is identical for MODIS derived cloud optical properties.

368 A separate retrieval of the MAS values of optical thickness and effective radius was not
369 attempted in this work.

370 **4. Analysis of spectral albedo properties**

371 To test of the ability of single scattering models to accurately reproduce the observed
372 spectral albedo, we retrieved the optical thickness and effective radius using SSFR albedo
373 at two wavelengths from each spectrum coincident with the MAS flight legs. The
374 retrieved optical thickness and effective radius were then used to calculate the entire
375 spectrum with the radiative transfer model. The left-most plot in Figure 3a is the MAS
376 650 nm radiance for the $\mu=0.82$ case; time (UTC) is along the y-axis, the cross-track
377 swath of MAS along the x-axis. The second from the left, (3b) is the spectral albedo
378 measured by the SSFR. Wavelengths varies along the x-axis, time is on the y-axis. Note
379 the strong water vapor absorption in the measurements at 1400 nm and 1900 nm, and
380 weaker bands at 1140 and 940 nm, all represented by vertical bands in the image. Figure
381 4 shows a typical SSFR albedo spectrum with the water vapor band centers and band
382 widths shown to aid in interpreting the spectra. The third panel (Figure 3c) image is the
383 spectral albedo reconstructed from the 2-wavelength SSFR retrieval of the cloud optical

384 thickness and effective radius. The white bands are the aforementioned spectral gaps in
385 the ice-crystal model data (C5). There is little evidence of water vapor absorption in this
386 image. A comparison of the second and third panel images provides evidence that an
387 insufficient amount of water vapor was used in the model but it is of no consequence in
388 the present analysis because those bands were avoided in the retrievals. The image in the
389 bottom panel shows the difference between the reconstructed albedo and the SSFR
390 measured albedo. In this flight segment the optical thickness varied from 5 to 15 (see
391 figure 9 for the time series) and the effective radius varied from 25 to 35 μm . The
392 difference image varies little over this change in optical thickness and effective radius,
393 indicating that the single scattering optical properties given in C5 capture the range of
394 possible single scattering properties needed to accurately reproduce the spectral albedos
395 that were encountered during the flights examined here. Indeed, the difference plots for
396 the $\mu=0.88$ and $\mu=0.60$ cases (not shown) are virtually identical to the $\mu=0.82$ case shown
397 here. The $\mu=0.92$ case is somewhat different as will be discussed later in the paper when
398 examining individual spectra.

399 In general, the differences outside of strong molecular gaseous absorption bands
400 (which has not been varied from a standard tropical profile and is highly variable for
401 water vapor) falls within 0.05 of the measured albedo. All four cases examined here fall
402 within moderate to high optical thicknesses. For the cloud optical thicknesses examined
403 here, all substantially greater than unity, the spectral albedo is not sensitive to particle
404 shape [Wendisch *et al.*, 2005]. Instead the effects of absorption are amplified through
405 multiple scattering and the single scattering albedo becomes the important single
406 scattering property for accurately reproducing the spectral shape of the albedo.

407 In Figure 5 the differences for all times are plotted at each wavelength showing
408 the entire range of differences for all wavelengths (the small black dots that in aggregate
409 form a line). Superimposed (red diamonds) is the calculated mean albedo difference at
410 each wavelength. The albedo differences are typically less than 0.05, with some
411 exception. Many of largest deviations occur on the edges of strong molecular absorbers
412 such as the 1400 and 1900 nm water vapor wings or the strong oxygen band at 763 nm
413 and are the result of gaseous absorption.

414 The $\mu=0.88$ case is the most spatially uniform, albeit short in duration, of the
415 flight legs examined here; it has the smallest retrieved range and standard deviation in
416 optical thickness. In terms of determining systematic differences between model and
417 measurement, this is perhaps the best of the flight legs because spatial homogeneity is
418 greatest. Wavelength to wavelength consistency (spectral shape) is similar for all the
419 cases, although the variation within a particular wavelength may be greater ($\mu=0.92$) or
420 lesser ($\mu=0.82$). The differences at the shortest wavelengths could be explained by
421 differences in molecular scattering and/or the presence of aerosols. Because these errors
422 are typically less than 0.03, and close to measurement error, no further refinement of the
423 modeling was undertaken.

424 The exception to this is the $\mu=0.92$ that had optical thicknesses substantially
425 higher (33-46) than the other cases (3-15). At the shortest wavelengths the differences are
426 0.07-0.08. The spectral shape of the differences is similar to the others cases, but the
427 magnitude is greater. This is true only of the shorter wavelengths; for the wavelengths
428 longer than 1500 nm the agreement is within 0.02-0.03. The reason for this difference is
429 unresolved. The largest systematic difference between measurement and model in all

430 cases, outside of strong gas absorption, occurs in the 1200 to 1300 nm range. Although
431 this region does contain a relatively narrow collision band of oxygen at 1270 nm the
432 mismatch is much broader. This mismatch increases with increasing optical thickness,
433 and is most evident for the $\mu=0.92$ case that has substantially higher optical thickness
434 than the other cases. This may indicate that the single-scattering albedo is too high in this
435 spectral region as multiple scattering (high optical thickness) amplifies absorption. The
436 ice single-scattering properties in C4 and C5 used the *Warren* [1984] compilation for the
437 ice optical constants. A new compilation by *Warren and Brandt* [2008] contains
438 substantial changes in the near-infrared complex part of the index of refraction. These
439 changes have been implemented in the most recent single-scattering ice calculations from
440 the developers of C4 and C5, but were not available for this analysis.

441 A more detailed representation of the differences between the highest and lowest
442 retrieved values of optical thickness and effective radius (four in total) for each of the
443 four segments and its corresponding spectral albedo from SSFR is plotted in Figures 6
444 and 7. SSFR albedo spectra are plotted in black and are continuous; the red spectra were
445 the reconstructed using C5, and the blue spectra C4. The regions of best agreement are
446 from 1500 to 2100 nm, excluding the strong water vapor band at 1900nm. For the case
447 $\mu=0.92$, the high optical thickness and height of the cloud reduce the water vapor
448 absorption to the point where it ceases to interfere with the cloud albedo. This is because
449 the column water vapor above these high altitude clouds is low and the contribution of
450 water vapor absorption from below the cloud layer (due to its high optical thickness) is
451 small. In the lower optical thickness cases, we are seeing “through” the cloud layer and
452 the contribution of water vapor absorption from below the cloud layer is much greater.

453 The agreement is quite similar (0.02) to the surrounding spectrum where water vapor
454 does not interfere with the ice cloud albedo. Note that in all the cases, as the optical
455 thickness becomes larger, the mismatch between the modeled and measured spectra
456 becomes larger in the 1200-1300 nm spectral region.

457 The effective radii for the C5 based retrieval are smaller in general than those
458 from C4. The optical thicknesses are generally greater for C5 than C4. This is in
459 agreement with a comparison done for the MODIS 4 and MODIS 5 collections (based in
460 part on C4 for MODIS 4 and C5 for MODIS 5) by *Yang et al.*, [2007] that showed
461 average optical thickness is greater by 1.2 from C5 (MODIS 5 collection) and an average
462 greater effective radius from C4 (MODIS 4 collection) of 1.8 μm .

463 **5. Comparison of Irradiance and Radiance Derived Optical Properties**

464 The comparison of irradiance measurements (SSFR) and radiance (MAS) is
465 challenging for several reasons. Perhaps the greatest of these is the difference in spatial
466 sampling of the cloud field. MAS measures radiance over a finite swath width, 37 km at
467 the ground. The SSFR measures the cosine weighted radiance integrated over the upward
468 and downward hemispheres centered at the aircraft. To compare measurements from the
469 two instruments the MAS radiance is spatially averaged following the analysis of *Schmidt*
470 *et al.* [2007]. The technique averages MAS radiance over the half power point of the
471 SSFR signal. The diameter of the SSFR half power point is approximately the MAS
472 swath width, 17 km for a cloud deck at 10km and an ER-2 altitude of 20 km. Figure 8
473 shows the retrieved MAS optical thickness and effective radius from $\mu=0.88$. The circle
474 overlying the left part of the image represents the half-power region of an SSFR
475 measurement. For the times series of retrieved optical properties, Figure 8, the circle is

476 stepped down the image by one scan line, and a new average is calculated. This time
477 (flight) series of averages are compared for the two different instruments. Unlike the
478 SSFR, which uses measured downward irradiance to calculate the albedo, the MAS-
479 derived reflectance relies on absolute radiometric calibration and a top-of-atmosphere
480 solar irradiance spectrum.

481 In Figure 9 times series of retrieved optical thickness and effective radius are
482 shown for the four cases. For all cases, MAS optical thickness retrievals are greater than
483 those from SSFR; conversely, effective radius retrieved by SSFR is nearly always
484 greater. Because SSFR views an entire hemisphere, in nearly all cases this includes some
485 unknown fraction of open water. This could explain the consistent bias of higher optical
486 thickness retrieved by MAS relative to SSFR. In general these differences are small; the
487 average difference is 2-3 in optical thickness and 2-3 μm in effective radius. For short
488 periods of time the differences can reach up to 12. The largest absolute difference occurs
489 in the high optical thickness case $\mu=0.92$. As the optical thickness increases, the albedo
490 approaches its asymptotic limit. This means that small changes in albedo or reflectance
491 (or radiometric calibration) produce large changes in retrieved optical thickness. This is
492 consistent with the finding here that the largest differences in optical thickness were
493 found at relatively high values of optical thickness. A summary of the average
494 differences between the irradiance- and radiance-based retrievals and their standard
495 deviations is given in Table 1.

496 The variability of optical thickness and effective radius over a flight segment is
497 higher for MAS, indicating that even after averaging the MAS values, the radiative
498 smoothing from SSFR is greater still. This is not unexpected, as half the energy incident

499 on the SSFR originates from outside the swath of MAS. In addition, because the effects
500 of scattering are more pronounced at the shortest wavelengths (conservative scattering),
501 the variation in retrieved optical thickness is greater due to a greater contribution to the
502 signal from outside the view of MAS. Figure 10 shows the differences between
503 measured spectral albedo from SSFR from modeled spectral albedo derived using the
504 MAS-retrieved optical thickness and effective radius. The differences are greater than
505 those derived from the 2-wavelength SSFR retrievals (Fig. 5). The bias in optical
506 thickness retrieval produces a MAS-derived spectral albedo that is generally higher in the
507 visible. For the moderately absorbing spectral region from 1500 to 2100 nm the
508 differences are reduced and are generally within 0.05; for $\mu = 0.88$ case the differences are
509 even lower, between 0.01-0.02. Condensed water is weakly absorbing at these
510 wavelengths so scattering is reduced, resulting in smaller contributions from outside of
511 the MAS swath and better agreement. This is likely scene dependent, with the presence or
512 absence of clouds outside the MAS field of view also determining in part, the level of
513 agreement.

514 In Figure 11, the SSFR and MAS retrievals of optical thickness and effective
515 radius are compared for each case. The order is sequential in cosine of solar zenith angle:
516 the top row is $\mu = 0.60$, the bottom row $\mu = 0.92$. The left column shows comparisons of
517 retrieved optical thicknesses, the middle column the retrieved effective radii, and the right
518 column ratios of the effective radii retrieved by SSFR to that retrieved by MAS plotted
519 against the retrieved optical thickness from MAS. The plots of retrieved optical
520 thicknesses show a bias of higher optical thickness retrieved from MAS; this bias
521 increases as the optical thickness increases. This is most evident in the last row ($\mu = 0.92$)

522 where the optical thicknesses are 3-4 times greater than those in the other three cases and
523 deviation from the one to one line is substantial. The effective radius plots (center
524 column), also indicate a bias, as was stated previously, of larger effective radii retrieved
525 by SSFR. In the effective radii ratios versus optical thickness (right column), for optical
526 thicknesses less than 20 the differences in effective radii are large, up to 50%, (excluding
527 the brief departure of 200% in the $\mu=0.82$ case which may be the result of underlying
528 liquid water clouds). As the optical thickness increases the agreement in effective radius
529 becomes better. This is true in every case, even the high optical thickness case ($\mu=0.92$)
530 which agrees to within 10% at an optical thickness of 60 and is within 5% at an optical
531 thickness of 90. For all cases, the agreement is 10% or better when the optical thickness
532 is 22 or greater. For low optical thickness, the influence of surface albedo (dark ocean)
533 is greater, biasing the results to a larger effective radius. The MAS retrieval of cloud
534 optical properties, because it is spatially resolved, rejects pixels that are cloud free. As
535 optical thickness increases, in relatively planar ice clouds, the effects of cloud
536 heterogeneity and surface albedo are less of a factor and the agreement becomes better.
537 Despite the differences in the spatial averaging, and potential differences in radiometric
538 calibration, the MAS retrievals reproduce the observed spectral albedo to within 0.10
539 across the entire spectrum. In the most spatially uniform case ($\mu=0.88$) the differences
540 are considerably smaller. A radiometric offset between SSFR and MAS would also
541 contribute to the differences in the retrievals between the two instruments. Similar
542 comparisons to those presented in this study could be made with MODIS coverage to
543 provide a better spatial context with which to judge the total contribution of cloud to the
544 SSFR signal but would be hampered by differences in temporal sampling. The

545 coincidence of satellite, aircraft, and cloud conditions did not allow for such a
546 comparison in this study.

547 **6. Summary**

548 Optical remote sensing of the microphysical and optical properties of ice clouds from
549 satellites has focused on the retrieval of the two cloud properties necessary (but not
550 always to completely specify the inputs into radiative transfer models to recreate the
551 spectral albedo: cloud optical thickness and effective cloud particle radius. These
552 retrievals ultimately rely on models of bulk ice cloud single scattering properties of ice
553 particles to determine the values of optical thickness and effective radius. If the single
554 scattering parameters are correct or at least spectrally consistent and the retrieval is
555 robust, then the retrieval results can be used in radiative transfer models should correctly
556 recreate the spectral albedo. In the first part of this paper, a test the C5 and C4 libraries
557 of ice crystal single scattering properties was performed. The optical thickness and
558 effective radius were retrieved using a two-wavelength fit similar to that used by
559 satellites (MODIS) or its airborne proxy (MAS). The retrieved values were derived from
560 the SSFR measurements to remove biases due to spatial sampling differences between
561 SSFR and MAS. In addition, SSFR measures upwelling and downwelling irradiance,
562 reducing the errors that might occur from absolute radiometric calibration errors,
563 providing a more rigorous test of the model ice single scattering properties. The retrieved
564 effective radius and optical thickness were subsequently used to predict the measured
565 spectral albedo. The measured and modeled spectral albedo were found to be in very
566 good agreement, especially for the longer wavelengths (1500-2100 nm) where the albedo
567 differences were within 0.02-0.03 over the four flight segments, with a range in effective

568 radius from 25 to 40 μm . The optical thicknesses showed larger differences, yet still
569 produced differences between modeled and measured albedo spectra that were within
570 0.05. In general the disagreement was largest at shorter wavelengths, up to 0.09 for the
571 high optical thickness case ($\mu=0.92$) which may suggest a problem in the molecular
572 scattering component of the modeling or, less likely, the presence of aerosols. Ice
573 scattering properties may also be a source of error although at lower optical thickness the
574 model and measurements agree quite well. It is difficult to draw a firm conclusion based
575 on a single high optical thickness case. The greatest systematic discrepancy between the
576 measurements and models was for the wavelength region between 1200 nm and 1300 nm.
577 In the lowest optical thickness cases the agreement was consistent with adjacent spectral
578 bands. As the optical thickness increased, the differences were more pronounced. In the
579 highest optical thickness case, the albedo bias approached 0.10. The increasing error
580 with increasing optical thickness may suggest that the model single-scattering albedo is
581 too high in this spectral band. The increase in multiple scattering amplifies absorption
582 and could lead to a discrepancy such as is seen here.

583 In the second part of this paper we examined the retrievals from MAS, a satellite-
584 like sensor. The MAS retrievals of optical thickness and effective radius were used with
585 the radiative transfer model to predict the spectral albedo. This is a more challenging
586 task for two reasons: unlike the SSFR, the MAS instrument relies on its absolute
587 radiometric calibration to accurately predict reflectance and to determine optical
588 thickness and effective radius. It also measures radiance over a finite swath width,
589 whereas SSFR measures irradiance over a hemisphere. This introduces spatial sampling
590 differences which cannot be completely resolved. Nevertheless, averaging the derived

591 optical properties over the half-power point of SSFR, reproduces the majority of spectral
592 albedo to within 0.05 with the greatest differences occurring in the 400-1200 wavelength
593 range where scattering is greatest and the differences in spatially sampling are
594 exacerbated. For the longer wavelengths, greater than 1500 nm, the agreement is better,
595 in the range of 0.03 or less. A comparison of the retrieved optical thickness and effective
596 radius from SSFR and MAS shows an average absolute deviation of 2.76 in optical
597 thickness and 2.24 μm in effective radius for the three cases of low to moderate optical
598 thickness. The high optical thickness case shows a much greater difference of 40.5 in
599 optical thickness and 1.3 μm in effective radius. At these high optical thicknesses, the
600 retrieval (optical thickness value) is highly sensitive to small changes in radiance
601 (irradiance) as albedo reaches its asymptotic limit. The differences are systematic
602 between MAS and SSFR with MAS nearly always retrieving a higher optical thickness
603 and SSFR nearly always retrieving a larger effective radius. This could be explained by a
604 radiometric calibration error; small differences in the radiometric calibration would
605 produce the largest changes in optical thickness when optical thickness is already high.
606 Additionally, the SSFR hemispherical field of view nearly always includes some fraction
607 of open water. This would also lead to SSFR retrieving a smaller optical thickness.
608 Spatial sampling differences prevent any definitive answer to this discrepancy, and in any
609 case, the overall effect is small when calculating spectral albedo.

610 The role of single scattering properties for ice crystals are crucial in satellite
611 retrievals of ice cloud properties and ultimately for radiative transfer calculations and
612 their inclusion in ice cloud modeling in climate models We have examined here the
613 spectral consistency of these properties within the solar spectrum and over a range of

614 solar zenith angles and optical thicknesses encountered during TC⁴. We have validated
615 the fidelity of the derived properties of optical thickness and effective radius based on ice
616 single scattering properties to recreate the spectral albedo when used in a radiative
617 transfer model. New models from the same authors of the single scattering properties
618 used here have been developed for ice crystals with varying surface morphologies, from
619 smooth to rough and substantially roughened ice crystals. These models will have
620 continuous spectral sampling over the range of the SSFR instrument. They also include
621 updated values for the ice optical constants, which have changed substantially in the near-
622 infrared [Baum, 2009 personal communication]. These new libraries will be compared
623 with the same cases shown here to determine their ability to accurately reproduce spectral
624 albedo and to examine the impact on the retrieval of ice cloud optical properties.

625

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628

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Table 1. Summary of optical thickness and effective radius for the four cases.

(μ)	MAS Optical Thickness [mean (standard deviation)]	MAS Effective Radius [mean (standard deviation)]	SSFR Optical Thickness [mean (standard deviation)]	SSFR Effective Radius [mean (standard deviation)]	Optical Thickness Difference (SSFR-MAS) [mean (standard deviation)]	Effective Radius Difference [mean (standard deviation)] (μm)
0.60	8.29(4.39)	27.95(4.05)	5.63(2.02)	30.43(2.53)	-2.67(2.55)	2.48(2.50)
0.82	12.49(5.53)	27.53(4.55)	7.64(2.47)	35.24(3.26)	-4.85(3.32)	7.71(3.11)
0.88	12.92(2.96)	35.74(0.63)	10.19(2.07)	36.93(0.63)	-2.73(1.07)	1.19(0.43)
0.92	80.42(7.47)	26.63(0.89)	39.92(2.65)	27.91(0.70)	-40.48(1.30)	1.28(0.07)

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810 Figure 2. The results of the C5 library in the radiative transfer calculations of albedo
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815 Figure 3. 2-D representations of the $\mu=0.82$ case. The first panel is MAS radiance at
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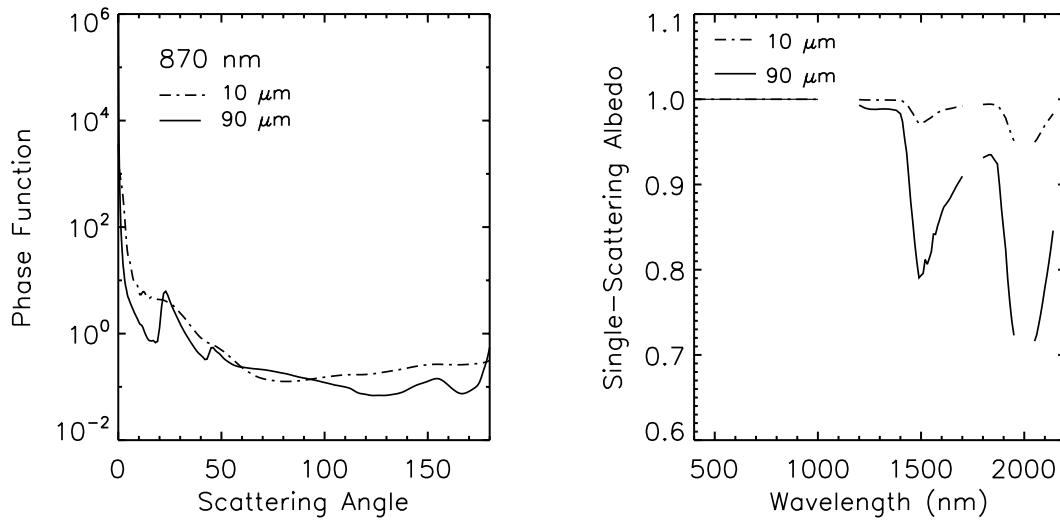


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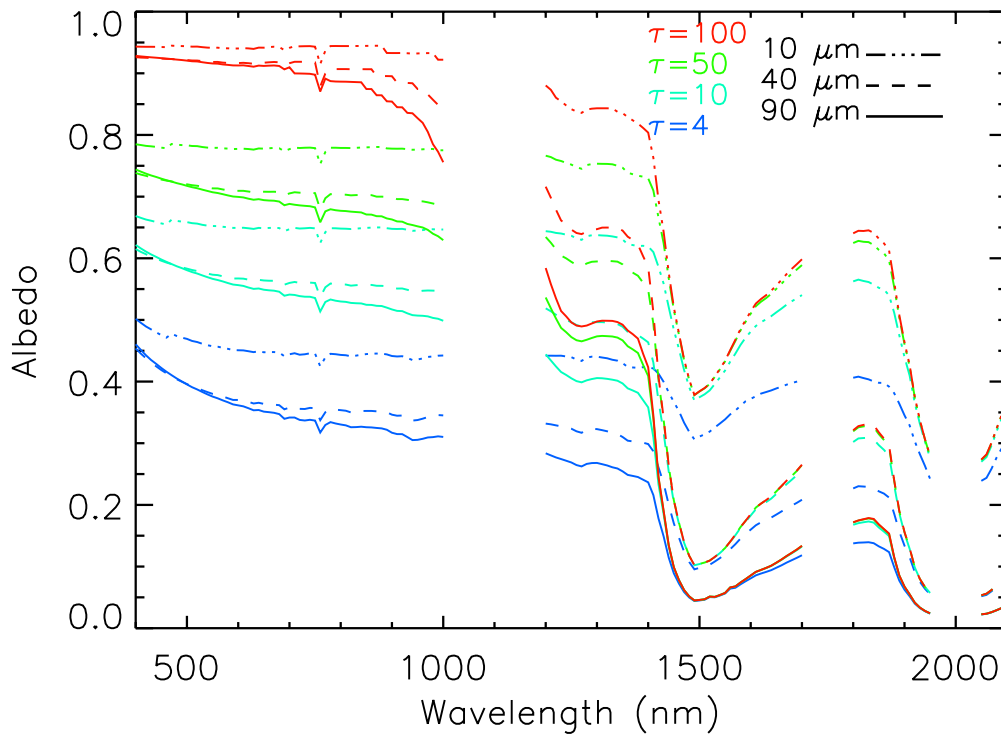


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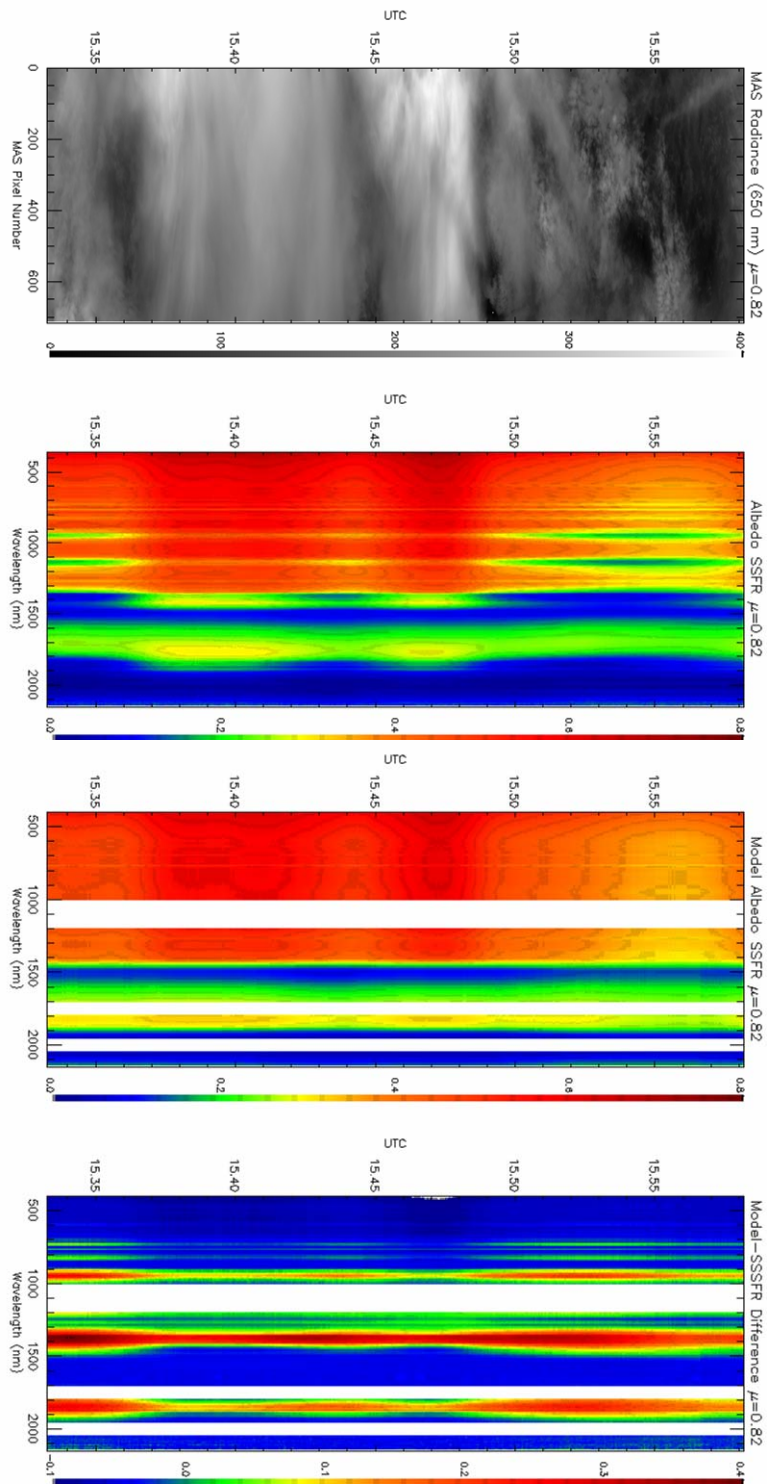


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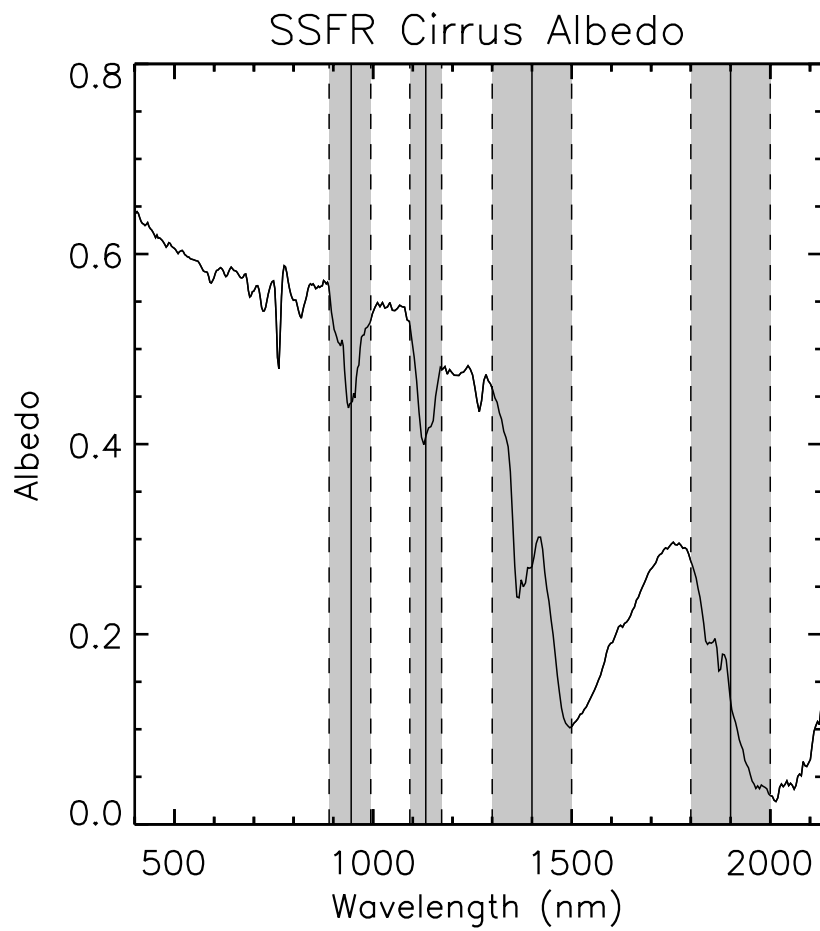


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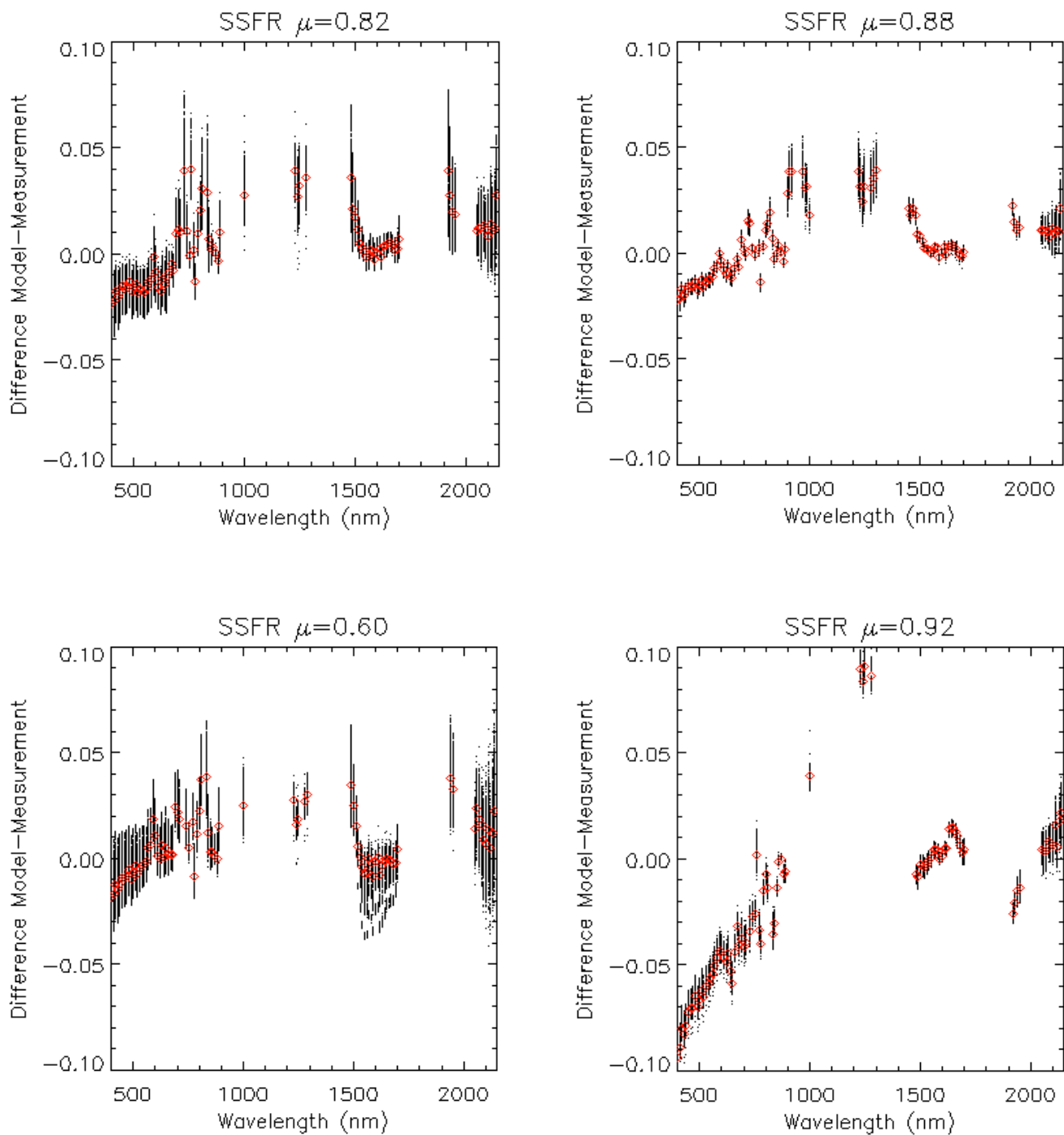
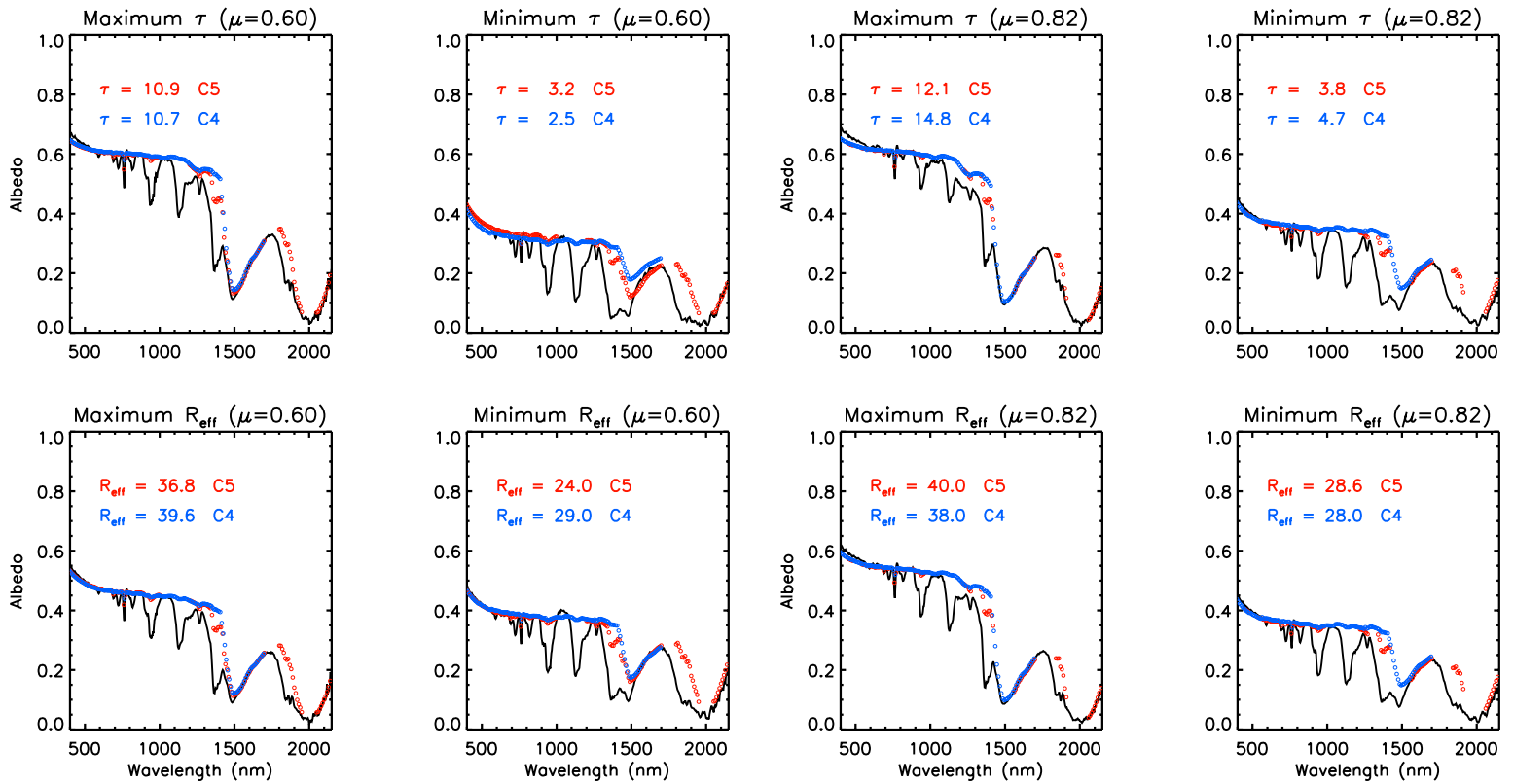


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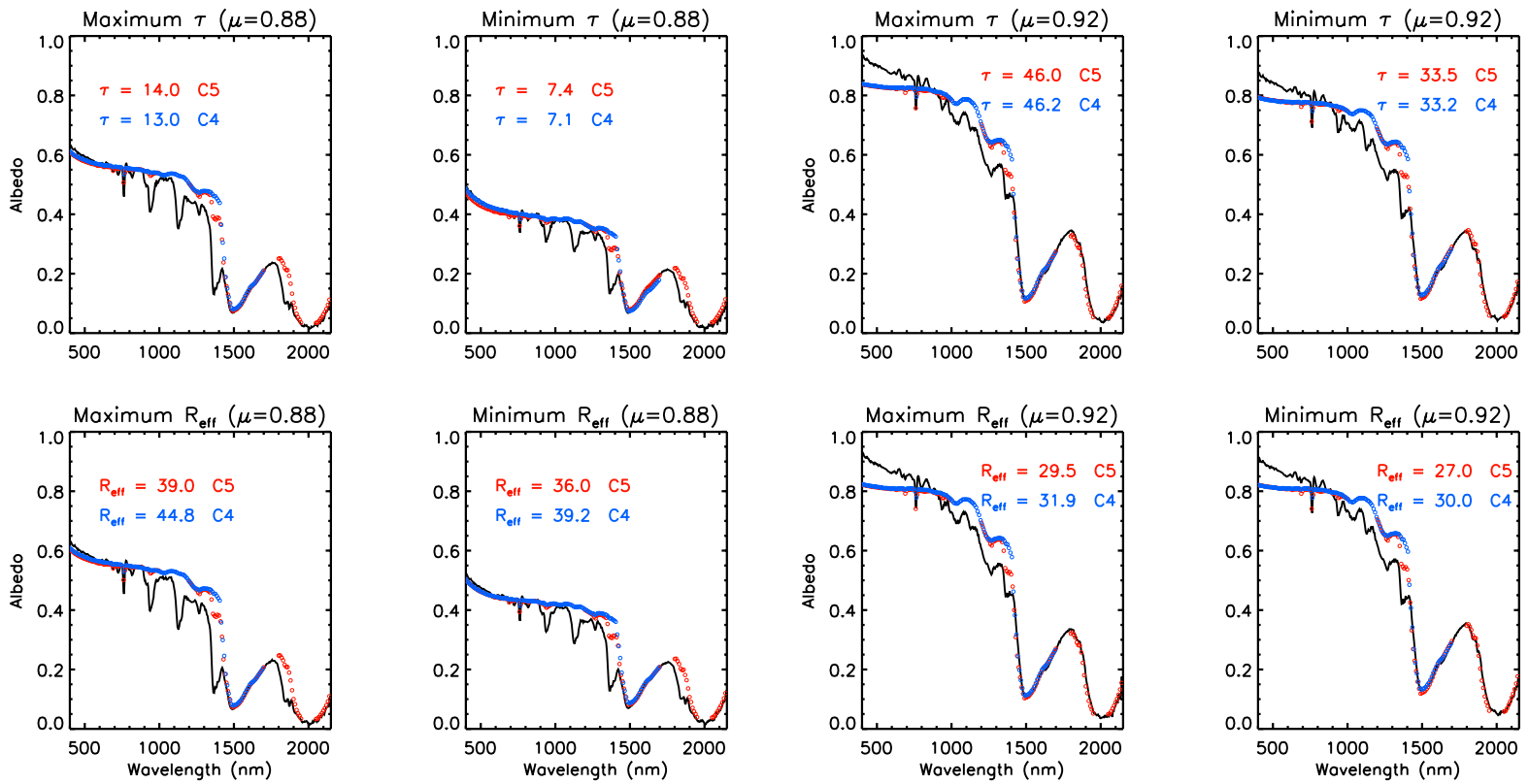


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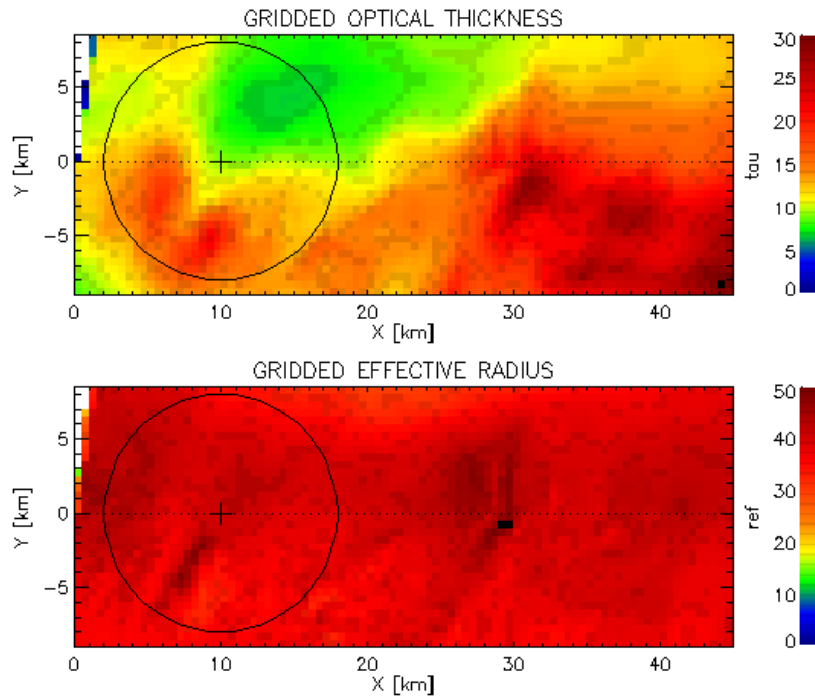


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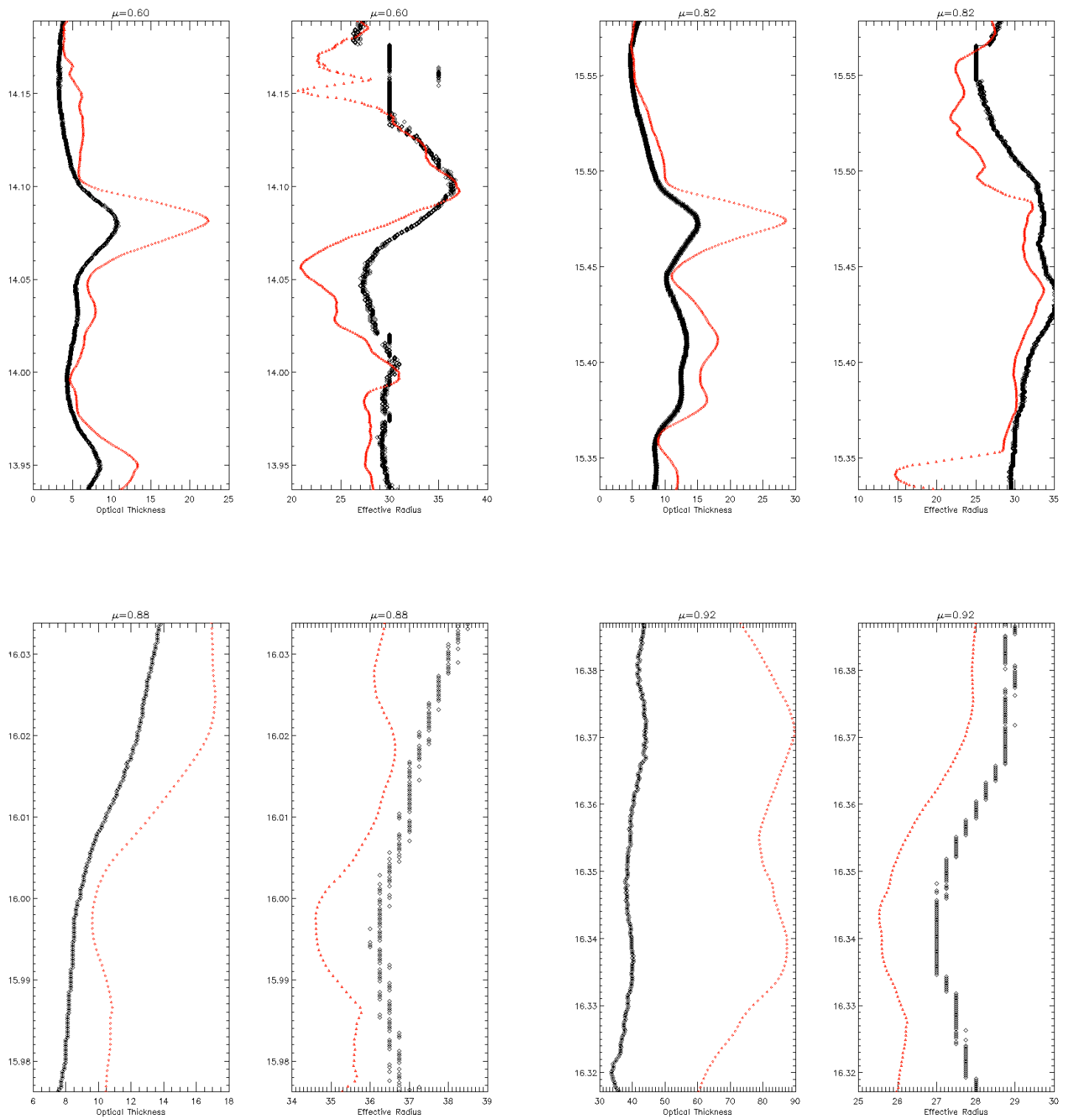


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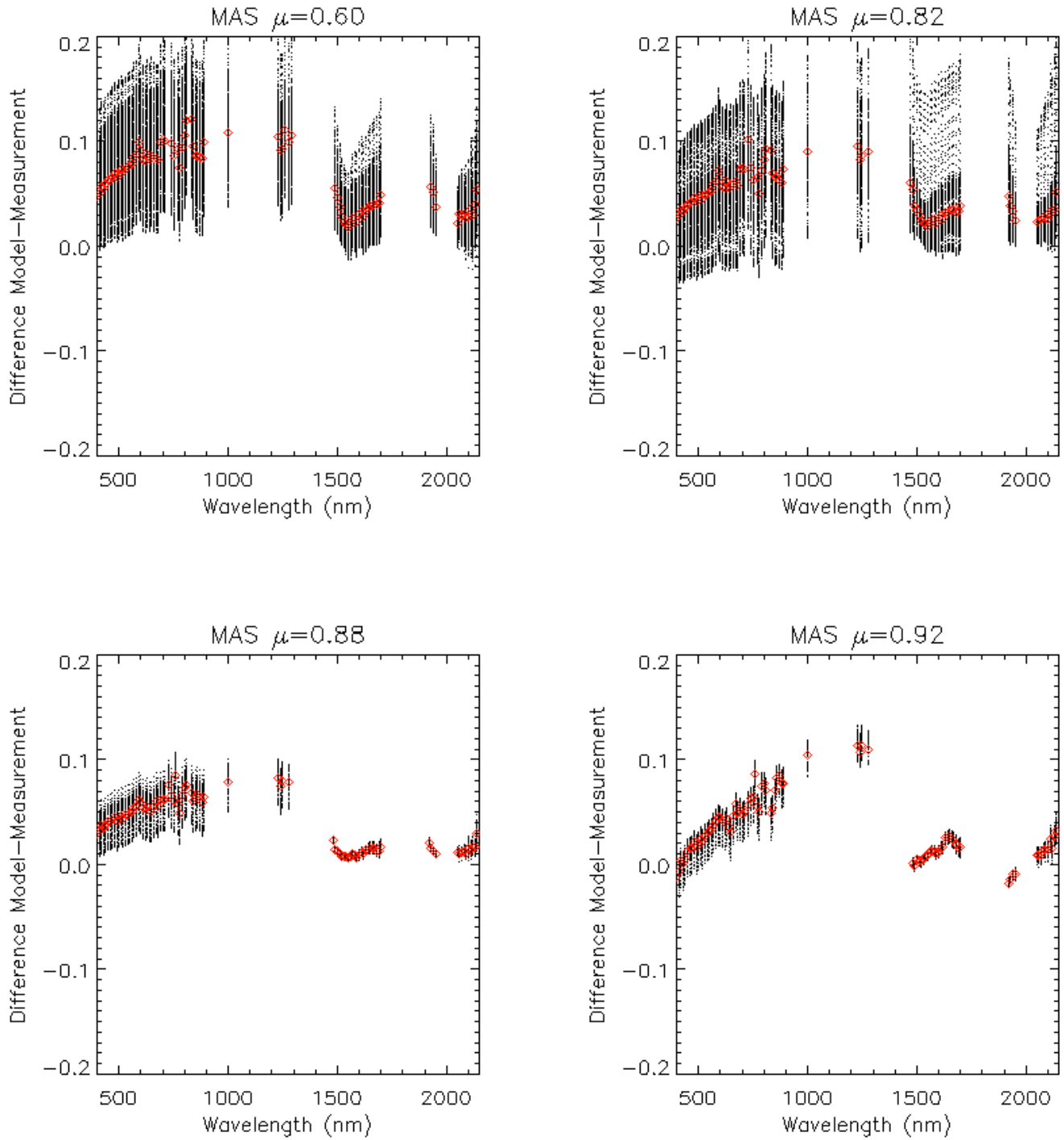


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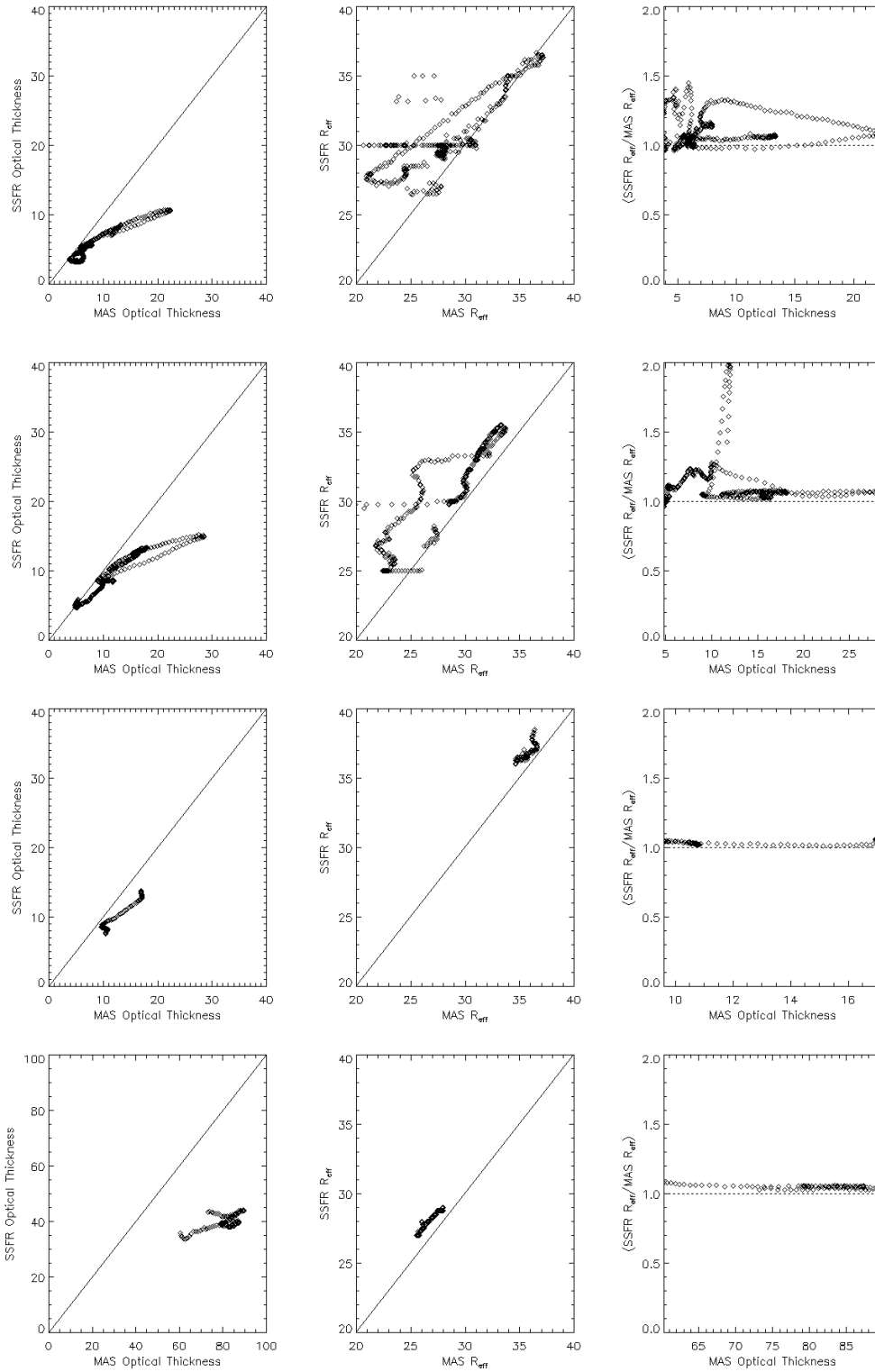


Figure 11. Optical thickness and effective radius as retrieved by SSFR and MAS are plotted against each other as is the ratio of effective radii from SSFR and MAS against optical thickness (third column). The top row is the $\mu=0.60$, the second row $\mu=0.82$, the third row $\mu=0.88$ and the bottom row is $\mu=0.92$. As optical thickness increases, the agreement between SSFR and MAS becomes better for effective radius.

